

Exploring the Modified IDEA

Using the `topicIDEA` Package

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Abstract

In the worksheet it has been shown how to use the IDEA algorithm for encryption 64/32/16-bit data with keys 832-bit or less.

1. Introduction

Normally, the IDEA operates on 64-bit blocks using a 128-bit user-selected secret key. Out of this 128-bit key fifty two key subblocks of 16-bit are generated and used in the encryption process. The 52 16-bit key subblocks needed in decryption are computed from the encryption key subblocks. In the modified mode of encryption/decryption by means of the IDEA algorithm the user does not select the 128-bit key but chooses directly the 52 16-bit key subblocks for encryption and employs them as a secret key. In this way IDEA can protect a 64-bit block of data using 832-bit key. By making this new secret key partly public we can encipher/decipher by means of the IDEA using a key of an arbitrary length, but no longer than 832 bits.

To use the `topicIDEA` package the user should download the files `topicIDEA.mla` and `topicIDEA.hdb` from the Maple Application Center [1], should place them in the directory having the name defined by the variable `dn`, and ought to execute the statements:

```
> restart:
dn := "g:/idea02":
#it is assumed that you store the package in the directory
"g:/idea02":
currentdir(dn);
march('open', "topicIDEA.mla"):
```

```

with(topicIDEA);

"
G:\idea02"

libname := "C:\Program Files\Maple 10\lib"topicIDEA.mla"

[A, HexS2bl, HexS2n16b, M, X, dbhist, i16cbcd, i16cbce,
  i16ecbd, i16ecbe, i32cbcd, i32cbce, i32ecbd, i32ecbe, i64cbcd,
  i64cbce, i64ecbd, i64ecbe, iddea, idea, idispks, iksb, iksd,
  iksgmd, iksgc1, iksgc2, iksgmd, ip24, ip42, ip48, ip84, mtf,
  sbdbarr, sbhist, up]

```

The worksheet **idea02.mw** should also be stored in the directory **dn**.

After carrying out the above statements, you may want to see the **topicIDEA** help page. If yes, execute:

```
> ?topicIDEA
```

We are now ready to test the modified mode of operation of the IDEA algorithm.

2. Modified Encryption/Decryption of 64-bit Block of Plaintext/Ciphertext - Examples

The first example concerns encryption with the 832-bit key:

```

> MD := 2^16:
n := 2:
printf("key length = %d%s",52*16, " bits");
key length = 832 bits

```

Now we generate at random a key schedule for encryption, playing the role of the 832-bit secret key, using the seed **123**:

```
> Z:=iksgmd(123);
```

```
Z := [ 52734 15725 28030 17730 61404 54370
      63206 15377  7763 63594 46203 58937
      23766 22241   96 55409 23166 53295
      53321  5664 33710 55520   111 36249
      17747 35662  3325 31140 14944 64720
      17476  7985 50999 45507 26626  6484
      49191 17730 55892 30255  6648 22461
      23728 17543 59241  4195  2428  8028
      3252 17766 28513 53461   0   0 ]
```

The encryption key schedule in hexadecimal notation:

```
> idispks(Z);
Key schedule:
round No. 1: CDFE 3D6D 6D7E 4542 EFDC D462
round No. 2: F6E6 3C11 1E53 F86A B47B E639
round No. 3: 5CD6 56E1 0060 D871 5A7E D02F
round No. 4: D049 1620 83AE D8E0 006F 8D99
round No. 5: 4553 8B4E 0CFD 79A4 3A60 FCD0
round No. 6: 4444 1F31 C737 B1C3 6802 1954
round No. 7: C027 4542 DA54 762F 19F8 57BD
round No. 8: 5CB0 4487 E769 1063 097C 1F5C
round No. 9: 0CB4 4566 6F61 D0D5
```

Let us use the message **Mersenne** as our plaintext block. Since the IDEA accepts four 16-bit plaintext subblocks, we must convert 8 bytes of the message into four subblocks:

```
> convert("Mersenne", bytes);
m := ip84(%); #see help page
m := [19813, 29299, 25966, 28261]
```

After doing it we are ready to encrypt the message represented by the variable **m** and to observe the encryption process:

```
> c := iddea(m);
input:          4D65 7273 656E 6E65
after round No. 1: EBCA 55D6 F6CC C801
after round No. 2: 5390 569A 2221 B591
```

```

after round No. 3: F79D A90F E486 AA7D
after round No. 4: 7EFC 7498 212B 8AF6
after round No. 5: 6A88 B1F2 A069 561E
after round No. 6: 612A 4932 FF5A 3577
after round No. 7: 9E2B 43FD DF57 C308
after round No. 8: B083 8E0E 0F4D 5854
output:           375A 54B3 FD6F 75D7
  c := [14170, 21683, 64879, 30167]

```

To decrypt the obtained cryptogram **c**, we need to determine the key schedule for decryption:

```
> Z := ikzd(Z);
```

```

Z := [38109 47770 37023 43183 2428 8028
      2472 6295 47993 64709 6648 22461
      20989 9644 47806 26074 26626 6484
      57343 14537 57551 25760 14944 64720
      41419 62211 29874 16178 111 36249
      51465 31826 59872 54166 23166 53295
      34947 65440 43295 32102 46203 58937
      731 57773 50159 13357 61404 54370
      12961 49811 37506 22426 0 0]

```

The key schedule for decryption in hexadecimal:

```
> idispks(Z);
```

Key schedule:

```

round No. 1: 94DD BA9A 909F A8AF 097C 1F5C
round No. 2: 09A8 1897 BB79 FCC5 19F8 57BD
round No. 3: 51FD 25AC BABE 65DA 6802 1954
round No. 4: DFFF 38C9 E0CF 64A0 3A60 FCD0
round No. 5: A1CB F303 74B2 3F32 006F 8D99
round No. 6: C909 7C52 E9E0 D396 5A7E D02F
round No. 7: 8883 FFA0 A91F 7D66 B47B E639
round No. 8: 02DB E1AD C3EF 342D EFDC D462
round No. 9: 32A1 C293 9282 579A

```

Here is the decryption process:

```

> mr := iddea(c);
input:          375A 54B3 FD6F 75D7
after round No. 1: F84D C6C0 8884 DF9D
after round No. 2: 0478 D9AE 8E74 922B
after round No. 3: 4FB8 67A0 D123 1B0E
after round No. 4: F552 2E28 FFE6 0991
after round No. 5: 6250 6834 BF2F 14F2
after round No. 6: 7C13 2281 AD7B E380
after round No. 7: 1015 151F 91E7 0657
after round No. 8: 6CF0 D2EC AFE0 912D
output:         4D65 7273 656E 6E65
  mr := [19813, 29299, 25966, 28261]

```

The retrieved plaintext block is correct:

```

> ip48(mr): #see help page
convert(%, bytes);

"
Mersenne"

```

Assume now that we publish the following key schedule for encryption:

```

> Z := Matrix(9, 6,
{(1, 1) = k[1], (1, 2) = 56312, (1, 3) = 53605,
(1, 4) = 60862, (1, 5) = 5819, (1, 6) = 21621,
(2, 1) = k[2], (2, 2) = 15830, (2, 3) = 61240,
(2, 4) = 39567, (2, 5) = 7420, (2, 6) = 8119,
(3, 1) = k[3], (3, 2) = 46749, (3, 3) = 32755,
(3, 4) = 30469, (3, 5) = 22510, (3, 6) = 45058,
(4, 1) = k[4], (4, 2) = 19673, (4, 3) = 13581,
(4, 4) = 24889, (4, 5) = 46192, (4, 6) = 34700,
(5, 1) = k[5], (5, 2) = 56701, (5, 3) = 25294,
(5, 4) = 51040, (5, 5) = 37454, (5, 6) = 8996,
(6, 1) = k[6], (6, 2) = 35369, (6, 3) = 25589,
(6, 4) = 64115, (6, 5) = 21144, (6, 6) = 8367,
(7, 1) = k[7], (7, 2) = 46961, (7, 3) = 20213,
(7, 4) = 55905, (7, 5) = 25923, (7, 6) = 31741,
(8, 1) = k[8], (8, 2) = 16401, (8, 3) = 33946,
(8, 4) = 25021, (8, 5) = 61848, (8, 6) = 36574,
(9, 1) = k[9], (9, 2) = 50601, (9, 3) = 36321,
(9, 4) = 16448, (9, 5) = 0, (9, 6) = 0}):

```

In the above case our choice of a secret key consists in determining nine 16-bit subblocks **k**. Evidently, the number of elements of the variable **k** may be arbitrary, but less than 53. Let

```
> k := [38157,55984,18626,55330,64243,1676,44249,18157,16858]:
printf("key length = %d%s",9*16, " bits");
key length = 144 bits
```

Here is the key schedule for encryption with the 144-bit secret key:

```
> idispks(Z);
Key schedule:
round No. 1: 950D DBF8 D165 EDBE 16BB 5475
round No. 2: DAB0 3DD6 EF38 9A8F 1CFC 1FB7
round No. 3: 48C2 B69D 7FF3 7705 57EE B002
round No. 4: D822 4CD9 350D 6139 B470 878C
round No. 5: FAF3 DD7D 62CE C760 924E 2324
round No. 6: 068C 8A29 63F5 FA73 5298 20AF
round No. 7: ACD9 B771 4EF5 DA61 6543 7BFD
round No. 8: 46ED 4011 849A 61BD F198 8EDE
round No. 9: 41DA C5A9 8DE1 4040
```

and the encryption process of the plaintext **2*17*59**::

```
> convert("2*17*59:", bytes);
m := ip84(%);
c := iddea(m);
[50, 42, 49, 55, 42, 53, 57, 58]

m := [12842, 12599, 10805, 14650]
```

```
input:          322A 3137 2A35 393A
after round No. 1: FD68 E61C 2DFD D53A
after round No. 2: 0459 F665 F106 AC5F
after round No. 3: 88EC AA23 295A B2E0
after round No. 4: 8B5E 0EF9 2187 B889
after round No. 5: EF22 E6EA 846E 4AB1
after round No. 6: 3D48 5950 DE3A B158
after round No. 7: 3C48 39CF D8C7 4317
after round No. 8: 8A1F BA8B 9C13 C0AD
output:         59DF 61BC 486C 3AE5

c := [23007, 25020, 18540, 15077]
```

The key schedule for decryption:

```
> Z := iksd(Z);
idispks(Z);
```

```
Z:=
[58551 14935 29215 65023 61848 36574
 3891 31590 49135 6983 25923 31741
56723 45323 18575 6321 21144 8367
 6061 39947 30167 61343 37454 8996
39150 40242 8835 11668 46192 34700
12848 51955 45863 60663 22510 45058
15816 32781 18787 39345 7420 8119
52125 4296 49706 34000 5819 21621
50632 9224 11931 39925 0 0]
```

Key schedule:

```
round No. 1: E4B7 3A57 721F FDFE F198 8EDE
round No. 2: 0F33 7B66 BFEF 1B47 6543 7BFD
round No. 3: DD93 B10B 488F 18B1 5298 20AF
round No. 4: 17AD 9C0B 75D7 EF9F 924E 2324
round No. 5: 98EE 9D32 2283 2D94 B470 878C
round No. 6: 3230 CAF3 B327 ECF7 57EE B002
round No. 7: 3DC8 800D 4963 99B1 1CFC 1FB7
round No. 8: CB9D 10C8 C22A 84D0 16BB 5475
round No. 9: C5C8 2408 2E9B 9BF5
```

Decryption process:

```
> mr := iddea(c);
ip48(mr);
convert(%, bytes);
```

```
input:          59DF 61BC 486C 3AE5
after round No. 1: 6DF5 5D61 79E0 255E
after round No. 2: 28A8 2D2F 10C1 8B11
after round No. 3: 8C7B E863 7113 1E71
after round No. 4: 8D9D 8455 EC76 22A9
after round No. 5: DBC0 5E67 F6FC 6FF2
after round No. 6: 5236 70F9 AD02 36B8
after round No. 7: EF09 1D35 23F2 7EAB
after round No. 8: E0EE FB9A 0D2F F5E8
output:         322A 3137 2A35 393A
```

```
mr := [12842, 12599, 10805, 14650]
```

```
[50, 42, 49, 55, 42, 53, 57, 58]
```

```
"  
2*17*59:"
```

```
> k := 'k': #the variable k will be used later
```

3. Modified Encryption/Decryption of 32-bit Block of Plaintext/Ciphertext - Examples

To encrypt/decrypt 32-bit blocks of plaintexts/ciphertexts we should execute:

```
> MD := 2^8:  
printf("key length = %d*s",52*8, " bits");  
key length = 416 bits
```

Now the key schedule consists of 52 8-bit subblocks and the maximal length of the modified secret key is now 416 bits.

```
> Z := iksgmd(12321);  
idispks(Z);
```

```
Z:= [ 225  39 172 133   3  14 ]  
     [ 252  93 192  97 111  24 ]  
     [  86 255 100  43 216 244 ]  
     [ 110 128 105 123  66 235 ]  
     [ 226  68  17 166 119 215 ]  
     [ 169  59  31 118  39  82 ]  
     [ 214 255 186 107  63  25 ]  
     [ 104 221 184 162 114  77 ]  
     [  77  40  19 114   0   0 ]
```

Key schedule:

```
round No. 1: E1 27 AC 85 03 0E  
round No. 2: FC 5D C0 61 6F 18  
round No. 3: 56 FF 64 2B D8 F4  
round No. 4: 6E 80 69 7B 42 EB  
round No. 5: E2 44 11 A6 77 D7  
round No. 6: A9 3B 1F 76 27 52
```



```

round No. 7: D6 FF BA 6B 3F 19
round No. 8: 68 DD B8 A2 72 4D
round No. 9: 4D 28 13 72

```

Let's follow the encryption:

```

> m := convert("1+2=", bytes);
c:= iddea(m);

```

```

m := [49, 43, 50, 61]

```

```

input:                31 2B 32 3D
after round No. 1:   32 0B D2 12
after round No. 2:   D6 43 44 E0
after round No. 3:   94 A1 D7 EE
after round No. 4:   D4 CD D8 10
after round No. 5:   90 17 90 D7
after round No. 6:   6B 76 12 F8
after round No. 7:   70 A5 D5 E1
after round No. 8:   CC 12 9B CC
output:              1F C3 25 7E

```

```

c := [31, 195, 37, 126]

```

Key schedule for decryption and decryption process:

```

> Z := ikzd(Z);
idispks(Z);
mr := iddea(c);
convert(%,bytes);

```

```

Z := [
247 216 237 124 114 77
215 72 35 211 63 25
251 70 1 245 39 82
73 225 197 159 119 215
58 239 188 48 66 235
250 151 128 140 216 244
3 156 1 6 111 24
154 64 163 53 3 14
8 217 84 143 0 0

```

Key schedule:

```

round No. 1: F7 D8 ED 7C 72 4D

```

```

round No. 2: D7 48 23 D3 3F 19
round No. 3: FB 46 01 F5 27 52
round No. 4: 49 E1 C5 9F 77 D7
round No. 5: 3A EF BC 30 42 EB
round No. 6: FA 97 80 8C D8 F4
round No. 7: 03 9C 01 06 6F 18
round No. 8: 9A 40 A3 35 03 0E
round No. 9: 08 D9 54 8F
input:          1F C3 25 7E
after round No. 1: 53 8D 82 D5
after round No. 2: 19 CC 75 41
after round No. 3: B2 AF 52 B8
after round No. 4: 6E E9 11 56
after round No. 5: 59 40 21 E9
after round No. 6: 9D A8 42 7B
after round No. 7: 07 92 68 CC
after round No. 8: E7 DE 52 92
output:        31 2B 32 3D

```

```

  mr := [49, 43, 50, 61]

```

```

"

```

```

1+2="

```

To reduce the length of a modified secret key we ought to partly announce the encryption key schedule. Thus, let

```

> Z := Matrix(9, 6,
  {(1, 1) = k[1], (1, 2) = 216, (1, 3) = 237,
  (1, 4) = 124, (1, 5) = 114, (1, 6) = 77,
  (2, 1) = 215, (2, 2) = k[2], (2, 3) = 35,
  (2, 4) = 211, (2, 5) = 63, (2, 6) = 25,
  (3, 1) = 251, (3, 2) = 70, (3, 3) = k[3],
  (3, 4) = 245, (3, 5) = 39, (3, 6) = 82,
  (4, 1) = 73, (4, 2) = 225, (4, 3) = 197,
  (4, 4) = k[4], (4, 5) = 119, (4, 6) = 215,
  (5, 1) = 58, (5, 2) = 239, (5, 3) = 188,
  (5, 4) = 48, (5, 5) = k[5], (5, 6) = 235,
  (6, 1) = 250, (6, 2) = 151, (6, 3) = 128,
  (6, 4) = 140, (6, 5) = 216, (6, 6) = k[6],
  (7, 1) = 3, (7, 2) = 156, (7, 3) = 1,
  (7, 4) = 6, (7, 5) = k[7], (7, 6) = 24,
  (8, 1) = 154, (8, 2) = 64, (8, 3) = 163,
  (8, 4) = k[8], (8, 5) = 3, (8, 6) = 14,
  (9, 1) = k[9], (9, 2) = k[10], (9, 3) = k[11],
  (9, 4) = 143, (9, 5) = 0, (9, 6) = 0}):

```

Our secret key is now determined by the variable **k**. Let:

```
> k := [118, 94, 155, 34, 225, 76, 168, 131, 106, 17, 6]:  
printf("key length = %d%s",11*8, " bits");  
key length = 88 bits
```

Encryption key schedule:

```
> idispks(Z);  
Key schedule:  
round No. 1: 76 D8 ED 7C 72 4D  
round No. 2: D7 5E 23 D3 3F 19  
round No. 3: FB 46 9B F5 27 52  
round No. 4: 49 E1 C5 22 77 D7  
round No. 5: 3A EF BC 30 E1 EB  
round No. 6: FA 97 80 8C D8 4C  
round No. 7: 03 9C 01 06 A8 18  
round No. 8: 9A 40 A3 83 03 0E  
round No. 9: 6A 11 06 8F
```

Encryption:

```
> m := convert("1+2=", bytes);  
c:= iddea(m);  
m := [49, 43, 50, 61]
```

```
input:          31 2B 32 3D  
after round No. 1: 9B 04 A0 CC  
after round No. 2: E9 86 19 06  
after round No. 3: DD F9 08 7D  
after round No. 4: B3 B9 CC 9C  
after round No. 5: 68 86 C4 4F  
after round No. 6: 33 5C 7E 6A  
after round No. 7: 15 F3 1E 9C  
after round No. 8: B4 E3 15 A3  
output:        3E 26 E9 B3  
c := [62, 38, 233, 179]
```

Decryption key schedule and decryption process:

```
> Z := ikzd(Z);  
idispks(Z);  
mr := iddea(c);  
convert(%,bytes);
```

$$Z := \begin{bmatrix} 177 & 239 & 250 & 133 & 3 & 14 \\ 252 & 93 & 192 & 206 & 168 & 24 \\ 86 & 255 & 100 & 43 & 216 & 76 \\ 110 & 128 & 105 & 123 & 225 & 235 \\ 226 & 68 & 17 & 166 & 119 & 215 \\ 169 & 59 & 31 & 189 & 39 & 82 \\ 214 & 101 & 186 & 107 & 63 & 25 \\ 104 & 221 & 162 & 162 & 114 & 77 \\ 159 & 40 & 19 & 114 & 0 & 0 \end{bmatrix}$$

Key schedule:

```

round No. 1: B1 EF FA 85 03 0E
round No. 2: FC 5D C0 CE A8 18
round No. 3: 56 FF 64 2B D8 4C
round No. 4: 6E 80 69 7B E1 EB
round No. 5: E2 44 11 A6 77 D7
round No. 6: A9 3B 1F BD 27 52
round No. 7: D6 65 BA 6B 3F 19
round No. 8: 68 DD A2 A2 72 4D
round No. 9: 9F 28 13 72
input:          3E 26 E9 B3
after round No. 1: 96 C1 33 85
after round No. 2: 99 7F F8 7A
after round No. 3: 2B 44 1D 09
after round No. 4: 66 88 A8 23
after round No. 5: C7 CD DA 8A
after round No. 6: 90 B4 CC B9
after round No. 7: AC C3 62 7D
after round No. 8: 80 1F 03 6F
output:        31 2B 32 3D

```

$mr := [49, 43, 50, 61]$

"

1+2="

4. Modified Encryption/Decryption of 16-bit Block of Plaintext/Ciphertext - Examples

It is possible to encrypt/decrypt 16-bit block (2 bytes) of plaintext/ciphertext after executing the statements:

```
> MD := 2^4:
printf("key = %d%s",52*4, " bits");
key = 208 bits
```

Let us observe the key schedule generation and encryption of the message **n!**. Since the IDEA accepts four 16-bit plaintext subblocks, we must convert 2 bytes of the message into four subblocks. After doing it we are ready to encrypt the message **m** and observe the encryption process:

```
> Z := iksgmd(123456789);
idispks(Z);
m := ip24(convert("n!", bytes));#see help page
c:= iddea(m);
```

```
Z:= [ 8 12  2  9 10 13
      12  7 10  4 15  3
      13 12  4  0  3 15
      4 14  2  4 11 15
      12  5 11  1  3 10
      8 15  7 10  5 14
      10  9  0 10  5  3
      14  0  0  3  8 15
      3 14  9  0  0  0]
```

Key schedule:

```
round No. 1: 8 C 2 9 A D
round No. 2: C 7 A 4 F 3
round No. 3: D C 4 0 3 F
round No. 4: 4 E 2 4 B F
round No. 5: C 5 B 1 3 A
round No. 6: 8 F 7 A 5 E
round No. 7: A 9 0 A 5 3
round No. 8: E 0 0 3 8 F
round No. 9: 3 E 9 0
```

```
m := [6, 14, 2, 1]
```

```
input:          6 E 2 1
after round No. 1: 7 D 2 1
after round No. 2: D 1 3 3
after round No. 3: 3 4 A 9
after round No. 4: 9 9 9 9
after round No. 5: D F F 8
after round No. 6: 0 4 B 9
after round No. 7: 4 8 1 9
after round No. 8: A E 6 4
output:         D 4 7 D
```

```
c := [13, 4, 7, 13]
```

```
> Z := iksd(Z);
mr := iddea(c);
convert(ip42(%), bytes); #see help page
```

```
Z := 
$$\begin{bmatrix} 6 & 2 & 7 & 0 & 8 & 15 \\ 11 & 0 & 0 & 6 & 5 & 3 \\ 12 & 0 & 7 & 12 & 5 & 14 \\ 15 & 9 & 1 & 12 & 3 & 10 \\ 10 & 5 & 11 & 1 & 11 & 15 \\ 13 & 14 & 2 & 13 & 3 & 15 \\ 4 & 12 & 4 & 0 & 15 & 3 \\ 10 & 6 & 9 & 13 & 10 & 13 \\ 15 & 4 & 14 & 2 & 0 & 0 \end{bmatrix}$$

```

```
input:          D 4 7 D
after round No. 1: 5 1 8 A
after round No. 2: 7 B D 5
after round No. 3: 2 6 E C
after round No. 4: 6 4 E 9
after round No. 5: C C 2 2
after round No. 6: 0 7 D E
after round No. 7: 0 C 4 4
after round No. 8: E 4 A 9
output:         6 E 2 1
```

```
mr := [6, 14, 2, 1]
```

"
n!"

The mode of encryption with the key less than 208 bits is left to the reader.

5. Conclusions

It has been shown that by putting to use the package named **topicIDEA** we can encrypt/decrypt with the IDEA more securely than usually. We may also construct many protocols offering the secret sharing and database encryption, by applying the presented here generalized method.

References

- [1] C. Koscielny: *The topicIDEA package*,
http://www.maplesoft.com/applications/app_center_view.aspx?AID=1922&CID=5&SCID=6
- [2] C. Koscielny: *The application of DES, IDEA and AES in strong encryption*, Quasigroups and Related Systems (accepted for publication in 2006)