Getting Started with Maple Toolboxes

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Preface

Introduction to the Toolboxes

Maplesoft™ offers a rich selection of add-on products. These toolboxes enhance and extend the power of Maple™ by adding solutions in specialized application areas, enhanced computation and deployment options, and connectivity with other technical tools. When taking advantage of these advanced products, you continue to have access to Maple's computational power, easy-to-use smart document interface, and rich technical documentation features.

• **BlockImporter™** allows you to import a Simulink® model into Maple, and convert it to a set of mathematical equations. Maple provides the power to simplify and manipulate the model, before simulating it in Maple or exporting it back to Simulink.

• The **Global Optimization Toolbox** provides world-class global optimization technology to return the best answer to your optimization model, robustly and efficiently.

• The **Grid Computing Toolbox** provides tools for performing Maple computations in parallel, allowing you to distribute computations across a network of workstations, a supercomputer, or the CPUs of a multiprocessor machine. It includes a personal grid server, allowing you to simulate and test your parallel applications before running them on a real grid network.

In This Manual

This manual provides an introduction to each of these toolboxes. Each section contains an overview of the toolbox, set-up details, getting started information, and examples.

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1 BlockImporter

1.1 Introduction to BlockImporter

Overview

BlockImporter allows you to import a Simulink model into Maple, and convert it to a set of mathematical equations. Maple provides the power to simplify, manipulate, and simulate the model.

Features of this toolbox include:

- The ability to perform calculations and simplifications on your Simulink models by using Maple's suite of tools.
- Perform advanced analysis on your systems by using Maple's built-in DynamicSystems package, including system object representation, graphical analysis, system manipulation procedures, signal generation tools, and system simulation.
- Reliable, tested computational routines to test the validity of your models, before performing simulations.
- Commands for performing frequency- and complex-domain analysis, stability and sensitivity analysis, and parameter optimization on your Simulink models.
- Symbolic methods for eliminating algebraic loops, which can significantly improve the efficiency and execution speed of your Simulink models.

Requirements

Before installing BlockImporter, you must install and activate Maple 15. You must also install MATLAB® and Simulink before using this toolbox. For details on supported Simulink versions and installation instructions, see the Install.html file on the product disc.

You need a purchase code to activate BlockImporter. This code has been emailed to you. If you have not received your purchase code, contact Maplesoft Customer Service at custservice@maplesoft.com (US and Canada), or the Maplesoft reseller in your region. For a list of resellers, visit http://www.maplesoft.com/contact/international/index.aspx.

After installation, the BlockImporter.mw file appears on your desktop (Windows® and Macintosh®) or in your home directory (Linux®). Open this file. Note that you can also access this file by entering ?BlockImporterTour in Maple.

The document BlockImporter.mw contains links to getting started documentation, help system documentation, and more. The getting started documentation contains an overview of the tools in this product, and provides multiple examples. The examples illustrate how to define a model in Simulink, import the mathematical model into Maple, and perform analyses such as stability, sensitivity, and parameter optimization.

1.2 Getting Started with BlockImporter

Establishing a Connection

To begin, open a new Maple window. Enter the following command to establish a connection with MATLAB.

> Matlab[openlink]();

A MATLAB command window should open. If one does not, follow the instructions in the Matlab/setup help page to configure the connection.

You are now ready to use BlockImporter.
Help with BlockImporter

For a list of commands in Maple to support BlockImporter, see the BlockImporter help page. Links to related Maple commands are also provided; many built-in Maple functions, especially the commands in the Dynamic Systems package, can be extremely helpful in generating and manipulating physical system models. For more information, refer to the DynamicSystems help page.

1.3 Working with BlockImporter

You can import any Simulink system or subsystem model by using the Import command. For more information, refer to the BlockImporter/Import help page.

1. Set the directory in which the Simulink files are located. For example, use the directory containing the pre-installed BlockImporter example models, which can be located by using the following command.

> datadir := BlockImporter[DataDirectory]() :

2. Using the Import command, specify the file to import. The inplace option indicates that the model will be converted in MATLAB to a Maple record. For more information, refer to the Record help page.

> with(BlockImporter)

[BuildDE, Import, PrintSummary, SimplifyModel] (1.1)

> sys := Import("example", path = datadir, init = "example_init", inplace = true) :

This particular model has the following model diagram in Simulink.

3. A copy of the model is created, consisting of a list of mathematical equations. Use the PrintSummary command to display the equations, variables, and parameters. For more information, refer to the BlockImporter/PrintSummary help page.

> PrintSummary(sys) :

Equations [24]:

![Model Diagram](image-url)
4. Use Maple's built-in simplification and simulation routines, especially those in the DynamicSystems package, to manipulate the model.

With the basic tools outlined here, you are now ready to use BlockImporter to create many engineering design solutions. See the Maple help system for more information about the commands used in this guide, or more ways in which BlockImporter can help you.
2 Global Optimization Toolbox

2.1 Introduction to the Global Optimization Toolbox

Overview

The Global Optimization Toolbox provides world-class global optimization technology to return the best answer to your optimization model, robustly and efficiently.

Features of this toolbox include:

• Several solver modules for nonlinear optimization problems, including branch-and-bound global search, global adaptive random search, multi-start based global random search, and a generalized reduced gradient local search.
• The ability to solve models with thousands of variables and constraints, with Maple's arbitrary precision capabilities in their calculations, to greatly reduce numerical instability.
• Support for arbitrary objective and constraint functions, including those defined in terms of special functions (for example, Bessel or hypergeometric), derivatives and integrals, piecewise functions, and Maple procedures.
• The interactive GlobalOptimization Assistant, an easy-to-use interface for entering your problem and choosing the solving method.
• Maple's built-in model visualization capabilities for viewing one- or two-dimensional subspace projections of the objective function, with visualization of the constraints as planes or lines on the objective surface.
• Global Optimization with Maple: An Introduction with Illustrative Examples by János D. Pintér is included.

Requirements

Before installing the Global Optimization Toolbox, you must install and activate Maple 15. For details and installation instructions, see the Install.html file on the product CD.

You need a purchase code to activate the Global Optimization Toolbox. This code has been emailed to you. If you have not received your purchase code, contact Maplesoft Customer Service at custservice@maplesoft.com (US and Canada), or the Maplesoft reseller in your region. For a list of resellers, visit http://www.maplesoft.com/contact/international/index.aspx.

After installation, enter ?GlobalOptimization in Maple to see an overview of the toolbox.

2.2 Getting Started with the Global Optimization Toolbox

Initialization

To start using the Global Optimization Toolbox, open a new Maple window and load the GlobalOptimization package by using the following command.

> with(GlobalOptimization);

> [GetLastSolution, GlobalSolve, Interactive] (2.1)
You can either use the commands to solve your pre-defined global optimization problem, or use the Global Optimization Assistant, shown below. The following examples demonstrate the use of the commands, but the assistant could also be used to solve any of the problems presented.

Help with the Global Optimization Toolbox

For help with the commands in the Global Optimization Toolbox, see the GlobalOptimization help page. You may also find the related commands in the built-in Optimization package helpful for solving optimization problems. For more information, refer to the Optimization help page.

2.3 Working with the Global Optimization Toolbox

In many optimization problems, simple methods are not sufficient to find the best solution. They will only find a local optimum, usually the one closest to the search starting point, which is often given by the user. For example, consider the expression $\ln(x) \cdot \sin(x)$. 
You could likely approximate the global minimum in the given domain, and find that minimum easily, by simply looking at the plot. But if you were unable to properly approximate it, or if you approximated incorrectly, you would not find the global minimum by using the usual optimization techniques.

\[ \text{Optimization}[\text{Minimize}](\ln(x) \cdot \sin(x), x = 1..50) \]

\[
\begin{align*}
[-3.39618690740209, [x = 29.8549920107437]]
\end{align*}
\] (2.2)

According to the Minimize command, the minimum is at approximately \( x = 30 \). However, you can see in the plot above that this is not the global minimum.

By using the global optimization equivalent of this command, you can be assured that you have found the global minimum in the specified interval.

\[ \text{with}(\text{GlobalOptimization}) : \]

\[ \text{GlobalSolve}(\ln(x) \cdot \sin(x), x = 1..50) \]

\[
\begin{align*}
[-3.88562417153593120, [x = 48.6999705692544]]
\end{align*}
\] (2.3)

To view the solving methods that were used to determine the global minimum, change the infolevel variable and re-execute the command. At infolevel = 3, the command displays the input model size and type, solver operational mode and parameter, and detailed runtime information.

\[ \text{infolevel}[\text{GlobalOptimization}] := 3 : \]
> **GlobalSolve**\((\ln(x) \cdot \sin(x), x = 1..50)\)

GlobalSolve: calling NLP solver  
SolveGeneral: calling global optimization solver  
SolveGeneral: number of problem variables 1  
SolveGeneral: number of nonlinear inequality constraints 0  
SolveGeneral: number of nonlinear equality constraints 0  
SolveGeneral: method multistart  
SolveGeneral: merit function evaluation limit 1000  
SolveGeneral: non-improving merit function evaluation limit 200  
SolveGeneral: constraint penalty multiplier 100.0  
SolveGeneral: target merit function value \(-0.10\times 10^{11}\)  
SolveGeneral: local search target objective function value \(-0.10\times 10^{11}\)  
SolveGeneral: local search feasibility tolerance \(0.10\times 10^{-5}\)  
SolveGeneral: local search optimality tolerance \(0.10\times 10^{-5}\)  
SolveGeneral: time limit in seconds 100  
SolveGeneral: trying evalhf mode  
SolveGeneral: total number of function evaluations 1120  
SolveGeneral: runtime in external solver 0.  
SolveGeneral: maximum constraint infeasibility 0.  
SolveGeneral: cycling or stall detected in solver  

\[ [ -3.88562417153593120, [ x = 48.6999705692544 ] ] \]

Typically, the *infolevel* is set to 0, the default.

> **infolevel**[GlobalOptimization] := 0:

The following is an example of a situation in which you cannot approximate the global minimum by using linear methods; however, the global solver finds the best solution.

**Example**

Consider a non-linear system of equations.

> \( eq1 := \sqrt{x^2 + y^2} + e^{x-y^2} + 5 \sin(2x - 4xy) - 12 \cos(xy) : \)

> \( eq2 := 5 \ln(1 + x^2) + e^{-y+x} + 5 \sin(6xy) : \)

The induced least-squares error function is highly multi-extremal, making it difficult to minimize the error of the least squares approximation.
To determine the global minimum of the least-squares error, define the objective function and constraints to be optimized.

\[ \text{objf := } eq1^2 + eq2^2 : \]

\[ \text{cons := } \{eq1, eq2\} : \]

First, try to find a local solution by using Maple's built-in \texttt{Optimization} package. This system is sufficiently complex that linear optimization solvers cannot find a feasible solution.

\[ \text{localsoln := Optimization[Minimize]}(\text{objf, } \{eq1 = 0, eq2 = 0\}, x = -1..2, y = -2..1) \]

\[ \text{Error, (in Optimization:-NLPSolve) no improved point could be found} \]

However, global optimization techniques can be used to find a global minimum.

\[ \text{sol := } \text{GlobalSolve}(\text{objf, } \{eq1 = 0, eq2 = 0\}, x = -1..2, y = -2..1) : \]

\[ \text{sol[1]; sol[2]} \]

\[ 5.24626533431424086 \times 10^{-23} \]

\[ [x = -0.558972497937727, y = 1.58234523718628] \] (2.5)

Substitution into the constraints shows that the least squares approximation can be a fairly precise solution. That is, the error of the least squares approximation is very small at the minimum point.
> eval(cons, sol[2])

\[
\{2.91588975187551 \times 10^{-12}, 6.63025190306143 \times 10^{-12}\}
\] (2.6)

With the examples demonstrated here, you are now ready to use the Global Optimization Toolbox to solve many complex mathematical problems. See the Maple help system for more information about the commands used in this guide, or more ways in which the Global Optimization Toolbox can help you.
3 Grid Computing Toolbox

3.1 Introduction to the Grid Computing Toolbox

Overview

The Grid Computing Toolbox provides tools for performing Maple computations in parallel, allowing you to distribute computations across a network of workstations, a supercomputer, or the CPUs of a multiprocessor machine. It includes a personal grid server, allowing you to simulate and test your parallel applications before running them on a real grid network.

Features of this toolbox include:

- A self-assembling grid in local networks, with an easy-to-use interactive interface for launching parallel jobs.
- Integration with job scheduling systems, such as PBS.
- High-level parallelization operations, such as map and seq, as well as a generic, parallel divide-and-conquer algorithm.
- Automatic deadlock detection and recovery.

Requirements

Before installing the Grid Computing Toolbox, you must install and activate Maple 15. For details and installation instructions, see the Install.html file on the product CD.

You need a purchase code to activate the Grid Computing Toolbox. This code has been emailed to you. If you have not received your purchase code, contact Maplesoft Customer Service at custservice@maplesoft.com (US and Canada), or the Maplesoft reseller in your region. For a list of resellers, visit http://www.maplesoft.com/contact/international/index.aspx.

Note that if you do not have a valid Grid license, the Grid Computing Toolbox will run in a limited capacity, allowing at most one server per machine and eight nodes in a job.

After installation, the GridComputing.mw file appears on your desktop (Windows and Macintosh) or in your home directory (Linux). Open this file.

3.2 Getting Started with the Grid Computing Toolbox

Establishing a Server and Network

You can run a server on your desktop machine to develop and test your parallel applications. The Personal Grid Server worksheet is an interactive Maple document that can help you start a personal server with any number of nodes. For more information, refer to the Grid/wks/PersonalGridServer help page.

The following Maple commands are a guideline for configuring your computer for a personal server. The given broadcast mask should ensure that you will not be added to any Grid networks. Note that these settings can be set by default. See the Install.html file for instructions. Configuration details can be found on the Grid/Properties help page.

> gridhost := "localhost";
> gridport := 2000:

> Grid[Setup]( "hpe", host = gridhost, port = gridport )

2000
To run Grid Computing applications on a network of machines, you must start Grid servers on each machine that you want to be part of the network. The toolbox will automatically detect new machines as they are added to the network, or you can turn off auto-discovery for use in a controlled environment, such as a PBS setup.

You will need to re-configure the Grid so that you can create or be added to a Grid network. Change the broadcastAddress and broadcastPort to your network's settings, and then start a server with those settings.

A few simple interactive examples using multiple nodes over multiple machines are in the Grid Computing worksheet. For more information, refer to the Grid/wks/Grid help page.

You are now ready to use the Grid Computing Toolbox, either on your own computer as a test server, or on a network of computers to run parallel applications.

**Help with Grid Computing**

For a list of commands in Maple to support the Grid Computing Toolbox, see the Grid help page.

### 3.3 Working with the Grid Computing Toolbox

As mentioned in the previous section, a few simple examples using multiple nodes over multiple machines can be found in the Grid Computing worksheet. For more information, refer to the Grid/wks/Grid help page.

The following provides a sample of the commands required to execute such examples. To begin, start a personal server using the local settings from the previous section, or use your network settings to connect with other computers running servers in the Grid Computing Toolbox. The code for this example can be found in the Grid Computing worksheet.

> with(Grid):

> Server[StartServer](port = 2000, numnodes = 4)

> 24417

(3.2)

Define the application or procedure that you want to perform, call it sampleCode. Then execute the following commands to deploy the application sampleCode over the network.

> fname := cat(kernelopts(toolboxdir = "Grid"), 
"/samples/Simple.mpl") :

> sampleCode := FileTools[Text][ReadFile](fname) :

> AvailableNodes := Status()[2]

> AvailableNodes := 4

(3.3)

> result := Launch(numnodes = AvailableNodes, sampleCode )

Node 2: This is node 2 out of 4  
Node 3: This is node 3 out of 4  
Node 0: This is node 0 out of 4  
Node 1: This is node 1 out of 4

result := [foo0bar, foo1bar, foo2bar, foo3bar]

(3.4)

When you are finished, make sure to close the connection before you close Maple, by executing the following command.
The following is a more detailed example of how you can use the Grid Computing Toolbox to create and perform parallel applications on a network of computers.

**Example**

Consider a fractal, specifically a Julia set, that you want to create and display in Maple. For any more than a few iterations, this can take a long time on a single computer. But you can divide the construction between an arbitrary sized network of computers by using the Grid Computing Toolbox.

First define a Julia set as a procedure, which will determine the color of the plot at point \((a, b)\). A Julia set is formally defined as

\[
\{ z \in \mathbb{C} \mid z_{i+1} = z_i^2 + c \text{ converges for } z_0 = z \}
\]

where \(c\) is a constant.

```maple
> JuliaSet := proc(a, b) global c1, c2;
local z1, z2, z1s, z2s, mr;
    (z1, z2) := (a, b);
    z1s := z1^2; z2s := z2^2;
    for m from 1 to 30 while z1s + z2s < 4 do
        (z1, z2) := (z1s - z2s + c1, 2*z1*s z2 + c2):
        z1s := z1^2; z2s := z2^2;
    end do;
    mr;
end proc:
```

Here it is assumed that for \(m\) over 30, the sequence \(z\) converges. Increasing this number will make the computation more accurate, but take much more time. Define the constant \(c = c1 + I c2\) and an appropriate view and grid size for this fractal. If \(c\) is changed, then \(v\) and gridsize may also need to be changed for the fractal to display properly.

```maple
> c1, c2 := -1.1107, .3089:
> v := [-1.7..1.6, -1..1]:
> gridsize := [250, 250]:
```

To display the fractal as a plot, use the Julia Set as the color. The procedure `plotsegment` displays the fractal, and is called by the nodes of the grid separately for each section of the plot.

```maple
> plotsegment := subs(js = eval(JuliaSet), proc(viewgrid)
plot3d(0, viewgrid[1], viewgrid[2], orientation = [-90, 0],
grid = viewgrid[3], style = patchnogrid,
scaling = constrained, color = js):
end proc):
```
Define the procedure to be run by the `Launch` command, which includes a procedure for splitting up the computation. For more information, refer to the `Grid/Launch` help page.

```pascal
> code := proc() local msg, split;
  split := proc(view, gridsize, n)
    local i, gs, splitview, viewi, viewrglobal vlength, vs;
    vs := op(view[1])[1];
    vlength := abs(op(view[1])[2] - op(view[1])[1]) / n;
    gs := floor(gridsize[1] / n);
    splitview := [vs..vs + vlength, view[2], [gs, gridsize[2]]];
    vs := vs + vlength;
    for i from 2 to n do
      if i = n then
        viewn := vs..op(view[1])[2];
        splitview := splitview, [viewn, view[2], [gridsize[1] - (n - 1) * gs, gridsize[2]]];
      else
        viewi := vs..vs + vlength;
        vs := vs + vlength;
        splitview := splitview, [viewi, view[2], [gs, gridsize[2]]];
      end if;
    end do;
  end proc;
  msg := Grid.Map(plotsegment, [split(v, gridsize, N)]);
  msg;
end proc;
```

Restart the Grid with your computer as the server, as in the above example. Configure the server for your network to run this example over a Grid.

```pascal
> Server[StartServer](port = 2000, numnodes = 4)

24525
(3.6)

> N := Status()[2]

N := 4
(3.7)
```

Now you are ready to perform the computation and display the results. Ensure that you pass all assigned variables to the `Launch` command, or they will not be available on the other nodes of the grid.

The printer is specified as `printf`, but could be any method of output, including writing to a text area component or a text file. The procedure provides a mechanism for you to stop the computation at any time, on all nodes. In this example, it is always false, so the computation cannot be stopped.

```pascal
> picture := Launch(code, numnodes = N, imports
  = ["plotsegment", "v", "gridsize", "JuliaSet", "c1", "c2", "N"]) :
```
With the basic tools shown here, you are now ready to use the Grid Computing Toolbox to solve many large mathematical problems. See the Maple help system for more information about the commands used in this guide, or more examples illustrating how the Grid Computing Toolbox can help you.